

Optimizers everywhere -

Optimization in Financial Applications with MATLAB

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Optimization

Definition of optimize in English:

optimize 🐠



1 Make the best or most effective use of (a situation or resource):

Optimum (disambiguation)

From Wikipedia, the free encyclopedia

The **optimum** is the best or most favorable condition, or the greatest amount or degree possible under specific sets of comparable circumstances.



Optimization in Financial Applications with MATLAB

Financial Optimization

Optimization Methods

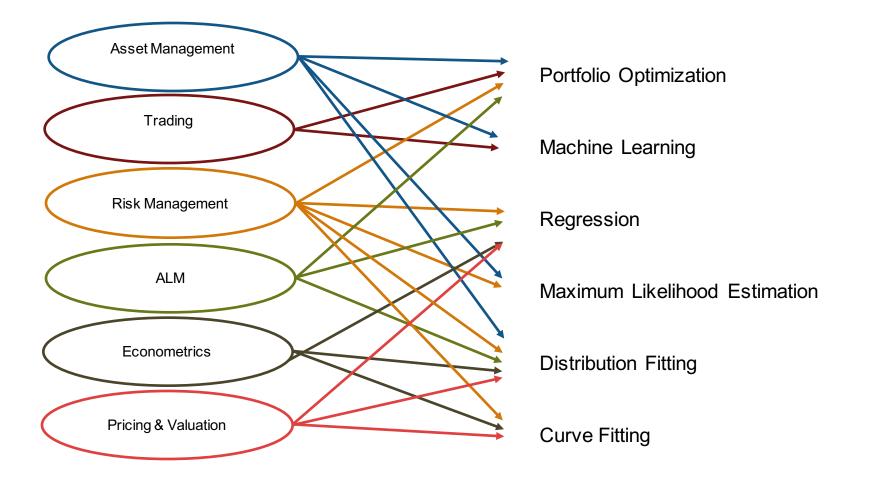
Customized optimization models



Financial Optimization

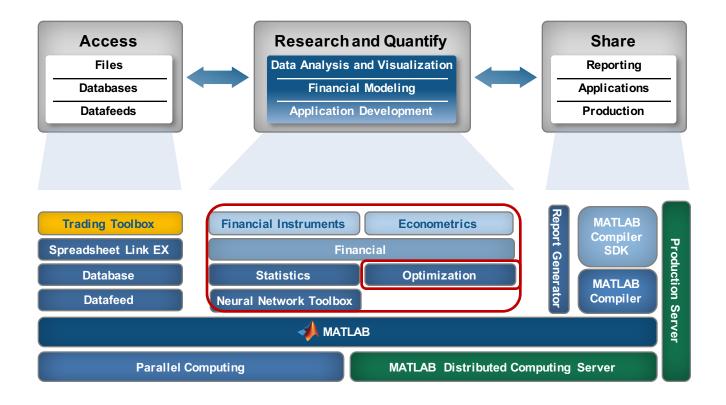


Financial Applications and Optimization



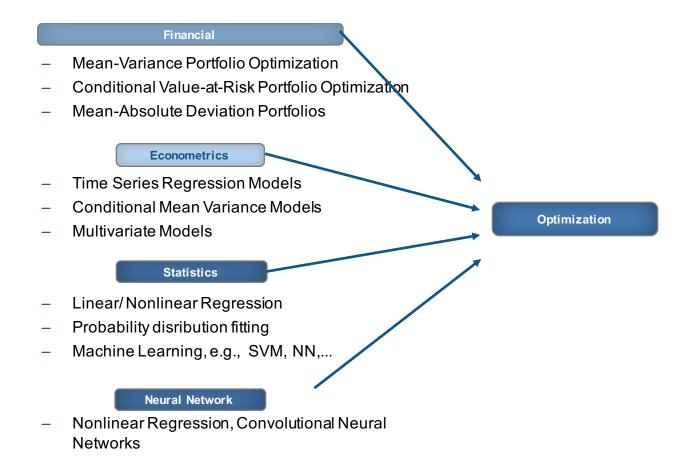


MATLAB – The Financial Development Platform





Financial Optimization within MATLAB

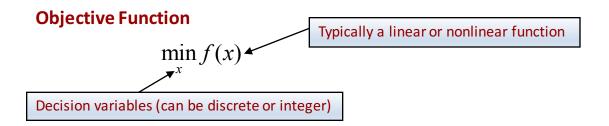




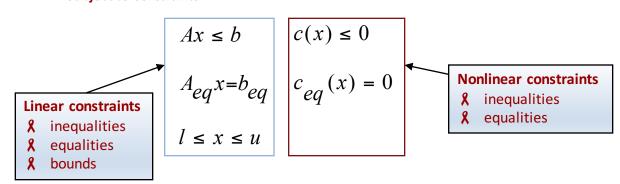
Optimization Methods



Optimization Problem



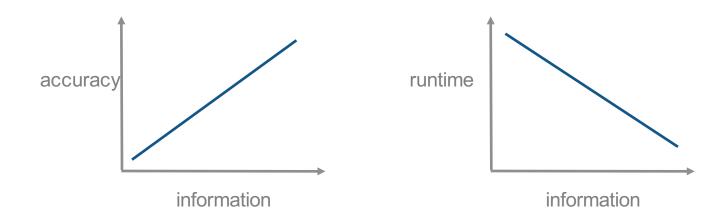
Subject to Constraints





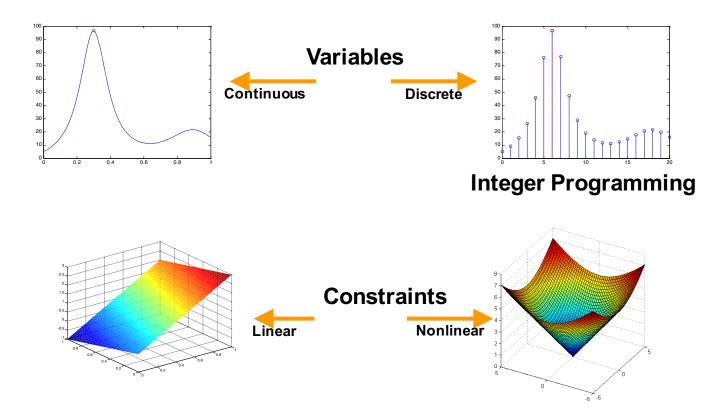
How to solve an optimization problem?

What do you know about your optimization problem?



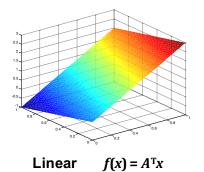


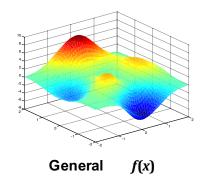
Variables & Constraints

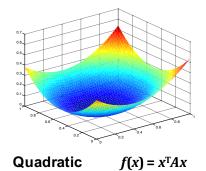


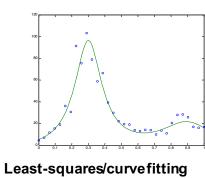


Objective Function





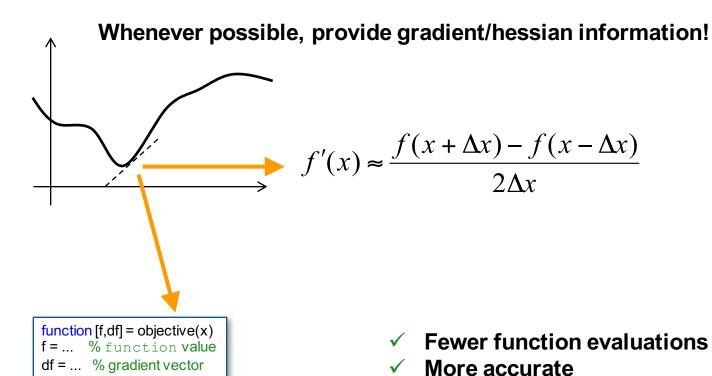




Least-squares/curve fitting $f(c) = \sum [g(x_k;c) - y_k]^2$



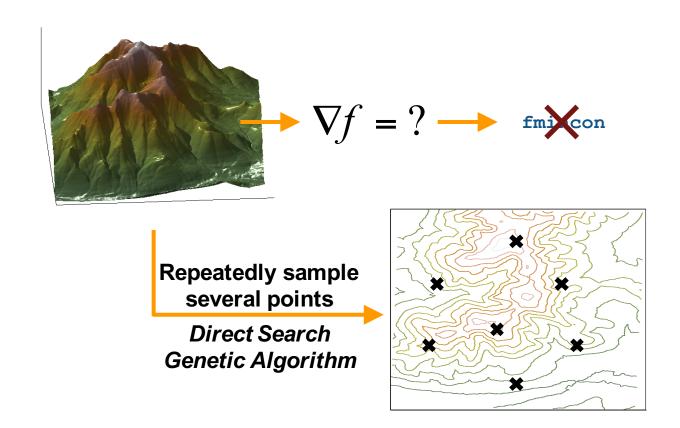
Numerical optimization



13



Derivative-Free Optimization





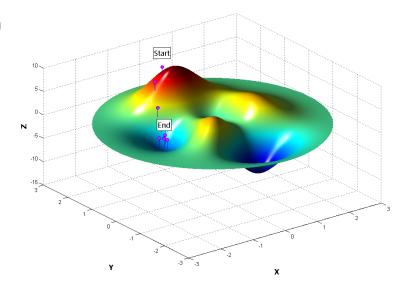
Approaches in MATLAB

Local Optimization

- Finds local minima/maxima
- X Uses supplied gradients or estimates them
- Applicable for large scale problems with smooth objective function
- Faster/fewer function evaluations

Global Optimization

- No gradient information required
- Solve problems with non-smooth, discontinuous objective function





Solvers

Variables

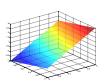


Continuous

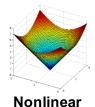


Discrete

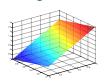
Constraints



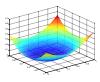
Linear



Objective function



 $f(x) = A^{\mathrm{T}}x$ Linear



Quadratic

 $f(x) = x^{T}Ax$



Least-squares $f(c)=\Sigma[g(x_k;c)-y_k]^2$

General f(x)

Solver

linprog

Optimization Toolbox

Documentation



Choosing the Algorithm

- · fmincon Algorithms
- · fsolve Algorithms
- · fminunc Algorithms
- · Least Squares Algorithms
- · Linear Programming Algorithms
- Quadratic Programming Algorithms
- · Large-Scale vs. Medium-Scale Algorithms
- · Potential Inaccuracy with Interior-Point Algorithms

fminunc

fmincon



Solvers

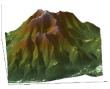
Variables

Continuous



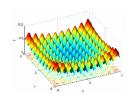
Discrete

Constraints



Non-smooth

Objective function



Nonlinear

Solver

Global Optimization Toolbox

Documentation



Choosing a Solver

Table for Choosing a Solver

There are seven Global Optimization Toolbox solvers:

- ga (genetic algorithm)
- GlobalSearch
- MultiStart
- patternsearch, also called direct search
- particleswarm
- · simulannealbnd (simulated annealing)
- gamultiobj, which is not a minimizer; see Multiobjective Optimization



Customized Optimization Models



Supported Portfolio Optimization Models

Financial Toolbox

- Mean-Variance Portfolio Optimization
- Conditional Value-at-Risk Portfolio Optimization
- Mean-Absolute Deviation Portfolio Optimization



Customized Objective - Smart Beta



Smart Beta Example – Risk Parity:

Generate a portfolio where each asset's marginal contribution to risk is equal

Marginal Contributions for N assets

$$MC_i(x) = x_i \times \frac{\sum_{j=1}^{N} x_j Cov(R_i, R_j)}{\sigma}$$

Minimize distance between all contributions

$$f(x) = \sum_{i=1}^{N} \sum_{i \neq i} |MC_i(x) - MC_j(x)|$$



Create marginal risk contributions

$$MC_i(x) = x_i \times \frac{\sum_{j=1}^{N} x_j Cov(R_i, R_j)}{\sigma}$$

- Create a distance matrix
- Minimize the total distance between all the contributions

$$f(x) = \sum_{i=1}^{N} \sum_{j \neq i} |MC_i(x) - MC_j(x)|$$

```
function out = riskCostFunction(wts , covMat)
% Cost function to get equal risk-contribution
% Build up all the marginal risk contributions
rMarg = zeros(size(wts));
for i = 1:length(rMarg)
    rMarg(i) = wts(i) * covMat(i,:) *wts';
end
% Build a distance matrix
 [xx,yy] = meshgrid(rMarg);
% Compute total distance between entries
out = sum(sum(abs(xx-yy)));
```



Smart Beta Example – Risk Parity:

$$\min_{x} f(x) := \sum_{i=1}^{N} \sum_{j \neq i} |MC_{i}(x) - MC_{j}(x)|$$
s.t.
$$x^{T} e = 1$$

$$\text{lb} \le x \le \text{ub}$$

→ Nonlinear objective function with linear equality and bound constraints



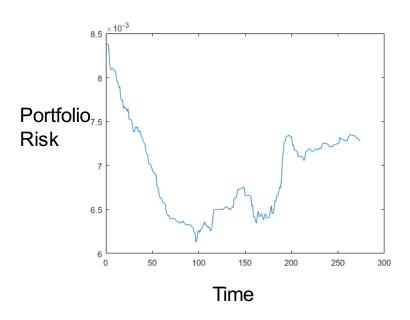
Solve with fmincon from MATLAB® Optimization Toolbox™

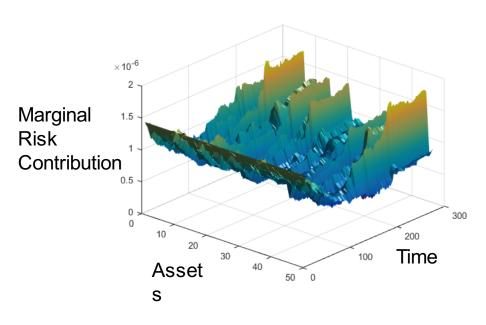
```
[fixWeights, fVal] = fmincon(@(x) riskCostFunction(x , covRet),... budget constraint

LB ,...

UB , [] , o);
```





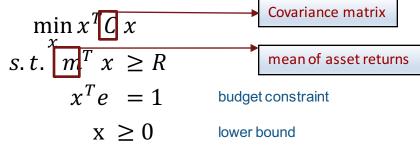




Customized Constraints - Robust Constraints



Mean-Variance Portfolio Optimization



Financial Toolbox



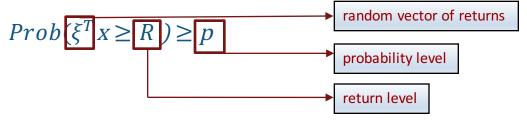
Additional constraints supported by

Financial Toolbox

- Linear inequality constraints
- Linear equality constraints
- Group constraints
- Group ratio constraints
- Average turnover constraints
- One-way turnover constraints



Extend standard model by individual constraints, e.g. robust constraints



→ Deterministic approximation (Chebychev's inequality)

$$m^{T}x - \sqrt{\frac{p}{1-p}}\sqrt{x^{T}Cx} \ge R$$
mean vector of returns
covariance of returns

P. Bonami, M.A. Lejeune, ,An Exact Solution Approach for Portfolio Optimization Problems Under Stochastic and Integer Constraints', Operations Research 2009, Vol. 57,Issue 3



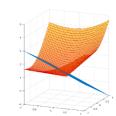
Mean-Variance Portfolio Optimization with robust constraint

$$\min_{x} f(x) \coloneqq x^T C \ x$$

$$s. \ t \qquad x^T e = 1 \qquad \text{budget constraint}$$

$$x \ge 0 \qquad \text{lower bound}$$

$$c(x) \coloneqq R - m^T \ x + \sqrt{\frac{p}{1-p}} \sqrt{x^T C x} \le 0 \qquad \text{robust constraint}$$



→ Robust mean variance model is a nonlinear, convex NLP



Solve with fmincon from MATLAB® Optimization Toolbox™



Provide gradients

```
options = optimoptions(@fmincon,...
'SpecifyObjectiveGradient',true,...
'SpecifyConstraintGradient',true,...
```

```
function [f,gradf] = quadObj(x,C)
f=x'*C*x; \longrightarrow f(x)
gradf = 2*C*x; \longrightarrow \nabla f(x)
end
```

```
function [c,ceq, gradC,gradCeq] = probConstr(x,p,m,C,R)

denom = sqrt(x'*C*x);

c = R - m'*x + p*denom; \longrightarrow c(x)
gradC = -m + p/denom*C*x; \longrightarrow \nabla c(x)
ceq = [];
gradCeq = [];
```

end



Provide Hessian

```
options = optimoptions(@fmincon,...
    'SpecifyObjectiveGradient',true,...
    'SpecifyConstraintGradient',true, ...
    'HessianFcn',@(x,lambda)getHessianRobustMV(x,lambda,C,p));
```

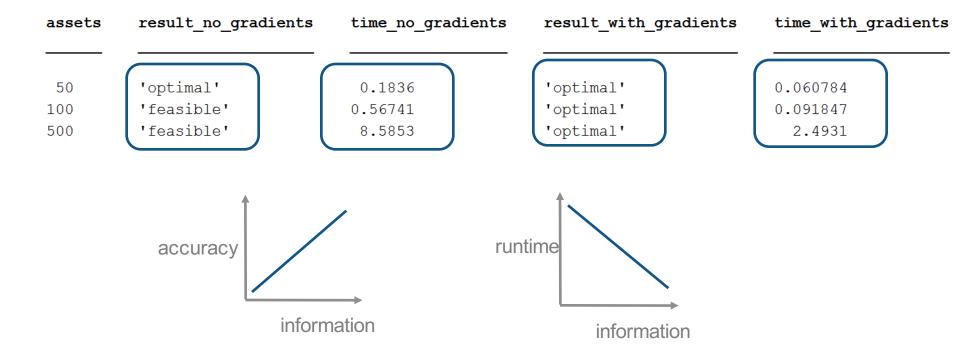
```
\nabla^2 f(x) + \sum \nabla^2 c_i(x) \cdot \lambda_i + \sum \nabla^2 ceq_j(x) \cdot \lambda_j
```

```
function H = getHessianRobustMV(x,lambda, C, p)

% This is the Hessian of
% objective function: quadObj
% constraint function: probConstr

sw = C*x;
dC = (p/sqrt(x'*C*x)).*(C-(sw*sw')./(x'*C*x));
dF = 2*C;
H = dF + lambda.ineqnonlin(1)*dC;
end
```







Without gradients

Iter f-count f(x) Feasibility optimality 0 51 6.098570e+01 2.400e+01 1.794e+02 1 102 1.881289e+01 1.757e+01 2.404e+02 2 153 8.850099e+00 1.172e+01 1.583e+02 3 204 2.926182e+00 5.126e+00 5.186e+01 4 255 1.599701e+00 2.437e+00 3.379e+00 5 306 1.269421e+00 5.720e-01 4.025e+00 6 358 1.249948e+00 3.610e-01 2.123e+00 7 409 1.279036e+00 1.805e-03 1.133e-01 8 460 1.042756e+00 9.026e-06 1.134e+00 9 511 5.778849e-01 6.602e-03 5.587e+00 10 562 4.839580e-01 9.742e-04 3.333e+00 11 613 4.824363e-01 9.517e-04 1.264e-01 12 664 3.615160e-01 4.711e-03 9.752e-01 13 <	$\overline{}$			0	
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9 511 5.778849e-01 6.602e-03 5.587e+00 10 562 4.839580e-01 9.742e-04 3.333e+00 11 613 4.824363e-01 9.517e-04 1.264e-01 12 664 3.615160e-01 4.711e-03 9.752e-01 13 715 3.328996e-01 1.925e-04 5.851e-02 14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	7	409	1.279036e+00	1.805e-03	1.133e-01
10 562 4.839580e-01 9.742e-04 3.333e+00 11 613 4.824363e-01 9.517e-04 1.264e-01 12 664 3.615160e-01 4.711e-03 9.752e-01 13 715 3.328996e-01 1.925e-04 5.851e-02 14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	8	460	1.042756e+00	9.026e-06	1.134e+00
11 613 4.824363e-01 9.517e-04 1.264e-01 12 664 3.615160e-01 4.711e-03 9.752e-01 13 715 3.328996e-01 1.925e-04 5.851e-02 14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	9	511	5.778849e-01	6.602e-03	5.587e+00
12 664 3.615160e-01 4.711e-03 9.752e-01 13 715 3.328996e-01 1.925e-04 5.851e-02 14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	10	562	4.839580e-01	9.742e-04	3.333e+00
13 715 3.328996e-01 1.925e-04 5.851e-02 14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	11	613	4.824363e-01	9.517e-04	1.264e-01
14 766 3.204592e-01 6.739e-05 9.337e-02 15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	12	664	3.615160e-01	4.711e-03	9.752e-01
15 817 3.150931e-01 1.709e-05 3.187e-02 16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	13	715	3.328996e-01	1.925e-04	5.851e-02
16 868 3.113085e-01 4.433e-12 3.139e-02 17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	14	766	3.204592e-01	6.739e-05	9.337e-02
17 919 3.108302e-01 1.244e-12 8.114e-03 18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	15	817	3.150931e-01	1.709e-05	3.187e-02
18 970 3.108004e-01 8.873e-13 2.088e-04 19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	16	868	3.113085e-01	4.433e-12	3.139e-02
19 1021 3.063753e-01 2.640e-13 5.799e-02 20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	17	919	3.108302e-01	1.244e-12	8.114e-03
20 1072 3.031614e-01 2.625e-05 7.867e-03 21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	18	970	3.108004e-01	8.873e-13	2.088e-04
21 1123 3.028625e-01 4.135e-06 4.636e-03 22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	19	1021	3.063753e-01	2.640e-13	5.799e-02
22 1174 3.028082e-01 5.297e-06 2.663e-03 23 1225 3.028131e-01 2.331e-15 3.900e-05	20	1072	3.031614e-01	2.625e-05	7.867e-03
23 1225 3.028131e-01 2.331e-15 3.900e-05	21	1123	3.028625e-01	4.135e-06	4.636e-03
	22	1174	3.028082e-01	5.297e-06	2.663e-03
24 1276 3.028131e-01 2.554e-15 3.637e-06	23	1225	3.028131e-01	2.331e-15	3.900e-05
	24	1276	3.028131e-01	2.554e-15	3.637e-06

With gradients

Iter	F-count	f(x)	Feasibility	optimality
0	1	6.098570e+01	2.400e+01	1.794e+02
1	2	2.322288e+01	1.430e+01	1.269e+02
2	3	5.419761e+00	5.911e+00	2.018e+01
3	4	1.732759e+00	2.237e+00	5.623e+00
4	6	1.413489e+00	1.431e+00	2.503e+00
5	7	1.217778e+00	1.372e-01	1.418e-01
6	8	8.718262e-01	6.861e-04	1.491e+00
7	9	5.448938e-01	5.936e-03	3.887e+00
8	10	4.831605e-01	4.820e-04	4.325e+00
9	11	3.815757e-01	3.713e-03	1.552e+00
10	12	3.480601e-01	4.921e-04	2.120e+00
11	13	3.301950e-01	1.063e-10	1.102e+00
12	14	3.211171e-01	5.814e-11	2.573e-02
13	15	3.117667e-01	9.545e-05	3.841e-03
14	16	3.108083e-01	1.701e-12	2.069e-04
15	17	3.061063e-01	2.869e-13	6.978e-03
16	18	3.046152e-01	3.464e-12	9.367e-05
17	19	3.029598e-01	2.707e-06	1.094e-02
18	20	3.028149e-01	1.588e-14	1.571e-06

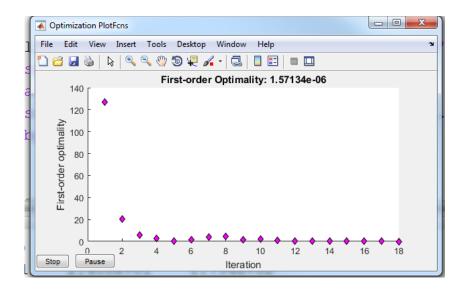


'PlotFcn', @optimplotfirstorderopt

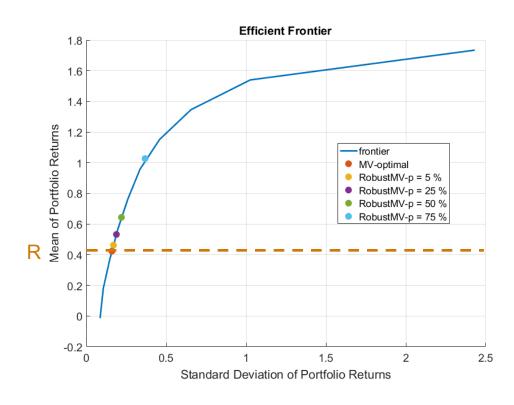
Without gradients

File Edit View Insert Tools Desktop Window Help First-order Optimality: 3.63712e-06 First-order Optimality: 3.63712e-06

With gradients

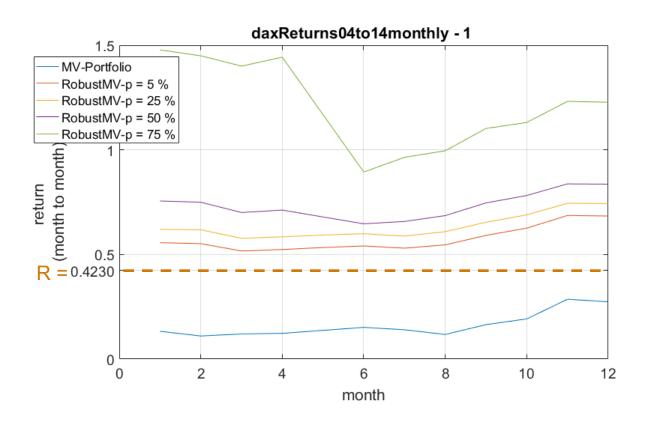






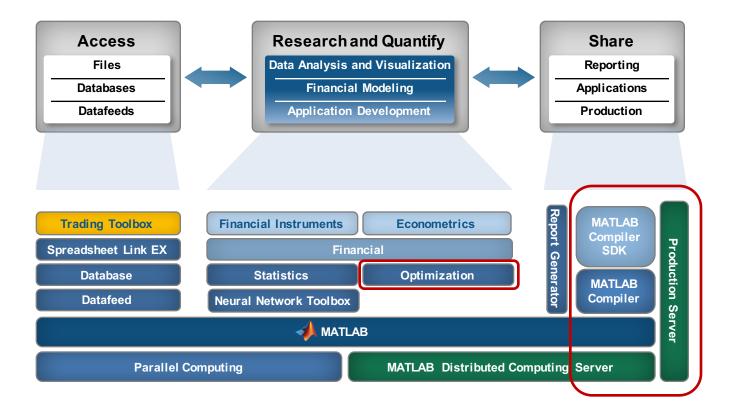


Customized Portfolio Optimization





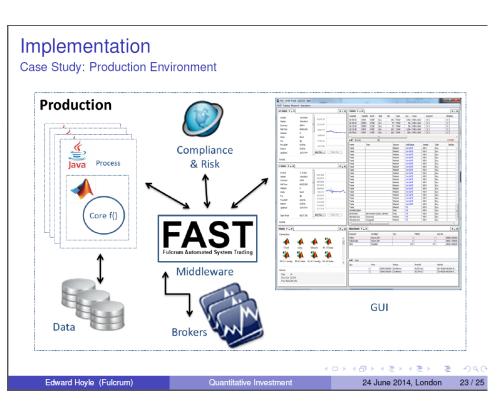
MATLAB – The Financial Development Platform





Customized Portfolio Optimization - Deployment

- Compile your MATLAB optimization model for your dedicated platform
- Make it available for your enterprise environment





Summary

- Optimization for financial applications is built within MATLAB toolboxes covering many standard applications
- A large variety of optimization algorithms available in MATLAB®
 Optimization Toolbox™ and Global Optimization Toolbox™
- Customized optimization models made easy by quick modeling, advanced optimization process diagnostics and rapid deployment.
- Enhance optimization performance and accuracy by adding maximal information.



Thank you!